

# **Facets of UNCERTAINTY**

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**STAHY '13**

**Areal distribution of extreme short rainfall  
evaluated using meteorological information**

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# OUTLINE

1. Possible weakness of short rainfall series used in standard regional analysis (Italian case).
2. Search regional rainfall homogeneity using atmospheric fields (\*)
3. Proposition of an areal distribution for maximum annual short rainfall of 1hour.
4. Vibo Valentia flood case study

(\*) S.Gabriele – Chiaravalloti F.

APPLICAZIONI METEOCLIMATICHE NELLA REGIONALIZZAZIONE DELLE PRECIPITAZIONI –pp 254 - CNR IRPI 2012  
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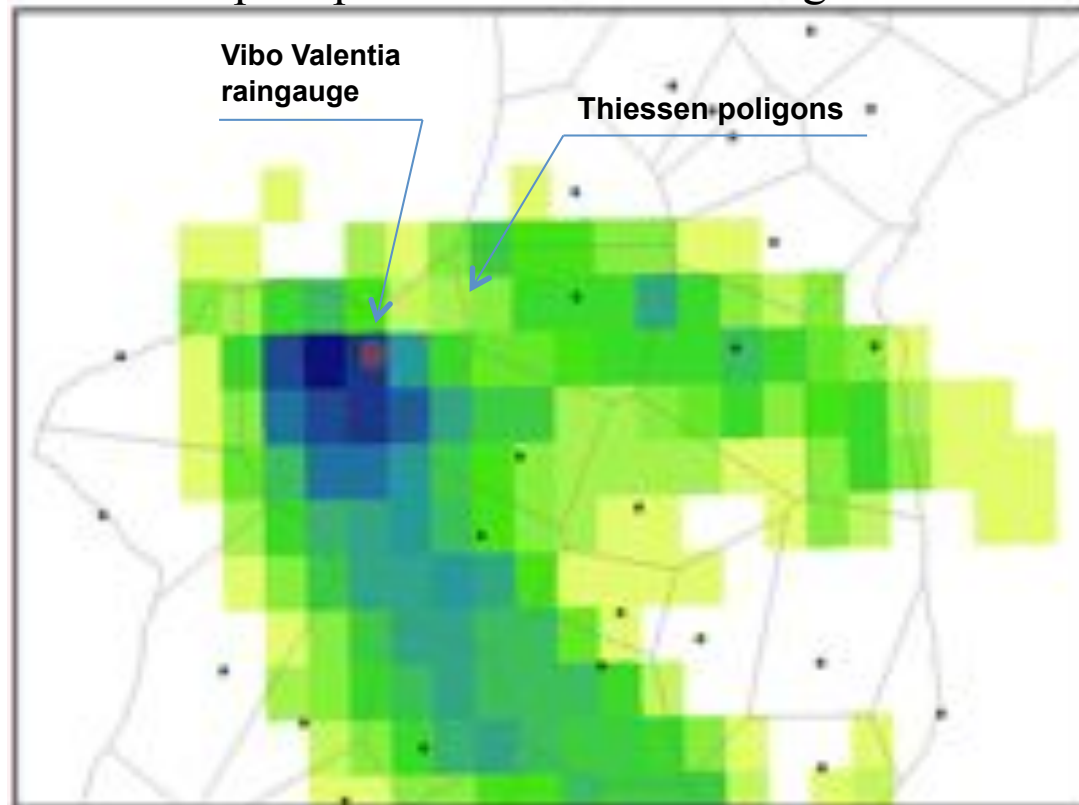
**Point 1** :Possible weakness of short rainfall series in standard regional analysis (Italian case).

### HOW ARE SIGNIFICANT THE HISTORICAL SERIES OF SHORT RAINFALLS (Calabria region, Italy)

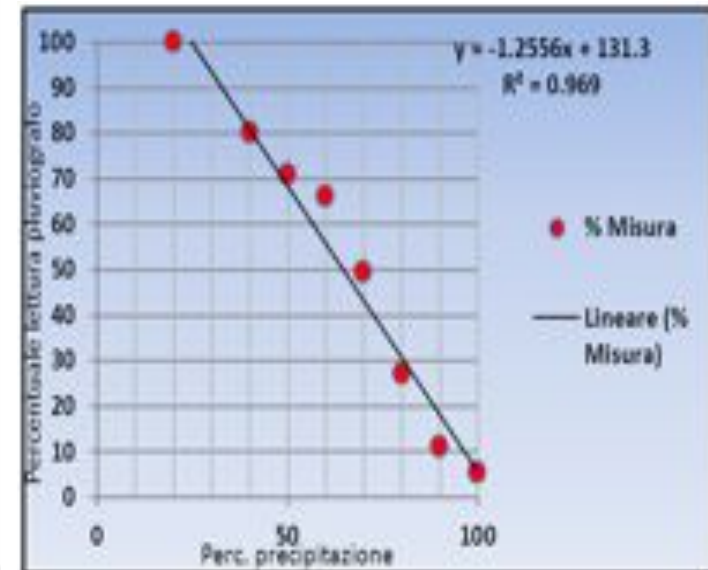
- Short heavy rainfall are mainly due to convective phenomena
- Core of convective cumulonimbus normally not exceed 15-25 kmq
- With a rain-gauge density of 1x200 kmq the probability to register the maximum intensity is about 10% which decrease with intensity

| Value | Percentu. |
|-------|-----------|
| 100   | 5.5       |
| 90    | 11        |
| 80    | 27        |
| 70    | 49.5      |
| 60    | 66.0      |
| 50    | 71.0      |
| 40    | 0.8       |
| 20    | 100       |

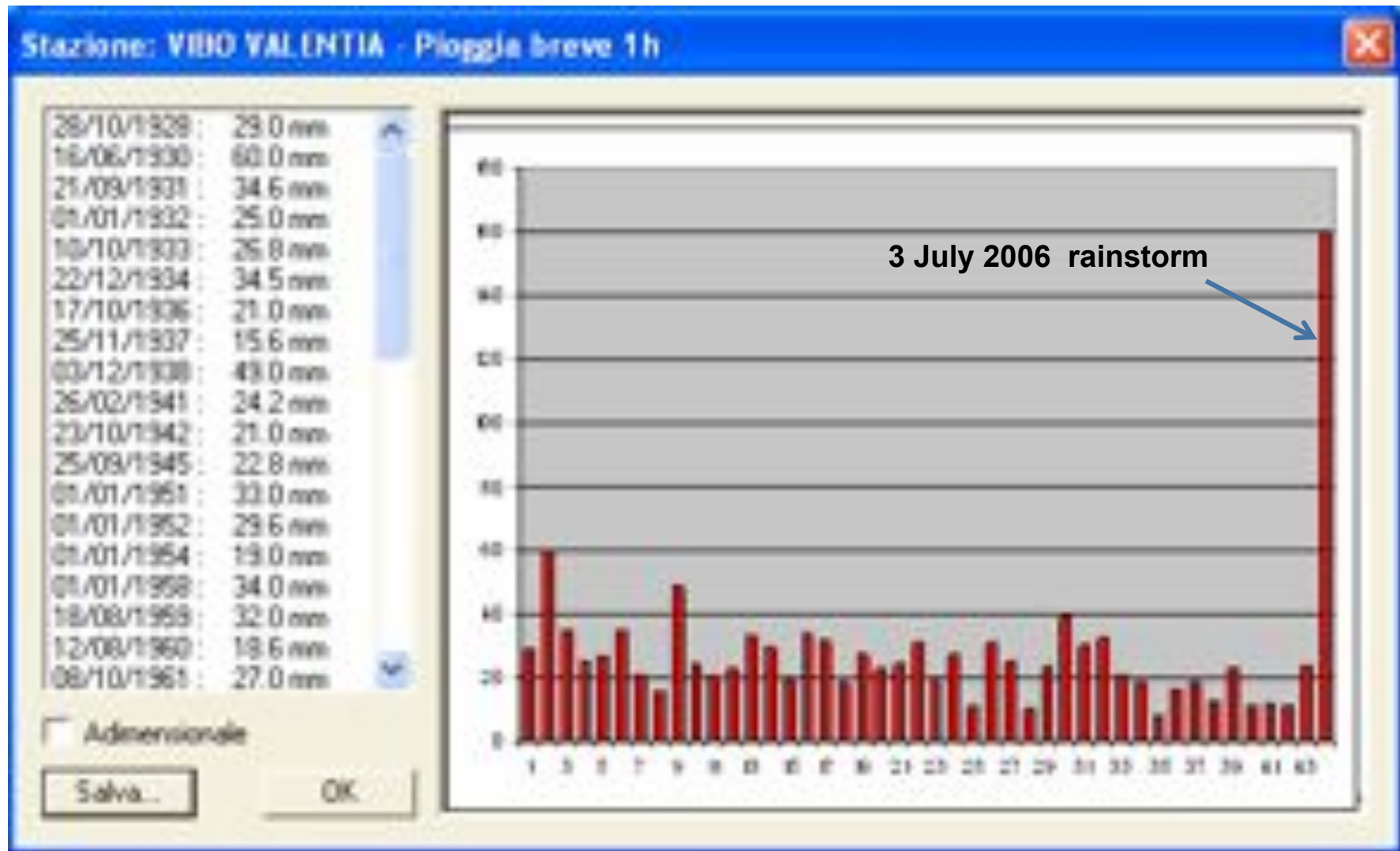
Total areal precipitations evaluated using MSG8



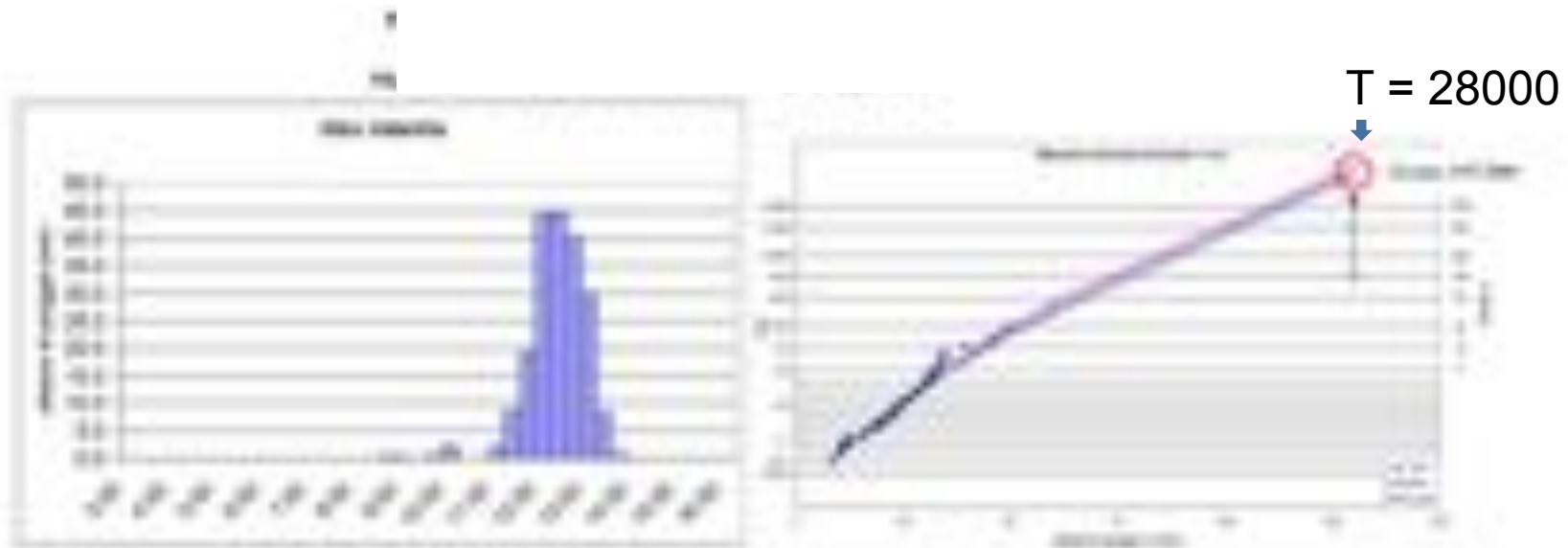
Percentage of precipitation versus rain gauge measure



# Vibo Valentia historical data for maximum annual rainfall of 1 hour



Evaluation of the Return Period for different rainfall duration, using two regional Models: VAPI and PAI based on the index method and TCEV distribution.



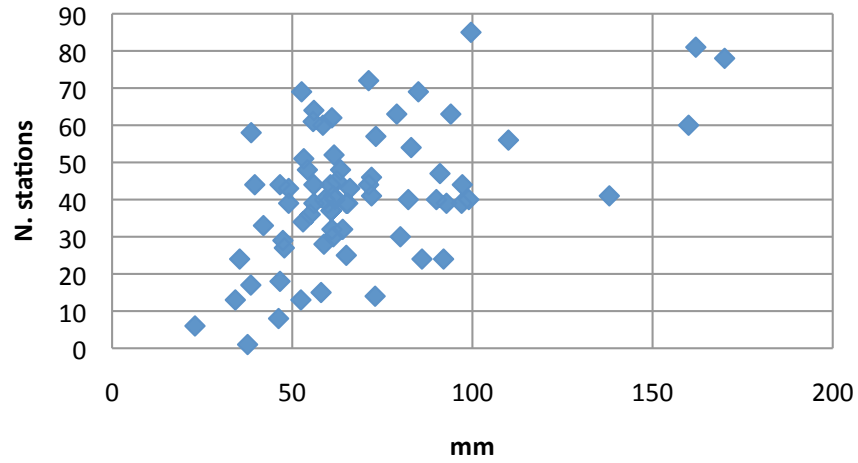
| Stazione        | Pioggia su 20 min |      | Pioggia su 1 h |       | Pioggia su 3 h |       | Pioggia su 6 h |       |
|-----------------|-------------------|------|----------------|-------|----------------|-------|----------------|-------|
|                 | PAI               | VAPI | PAI            | VAPI  | PAI            | VAPI  | PAI            | VAPI  |
| Mongiana        | 4                 | 4    | 1              | 1     | 1              | 1     | 1              | 1     |
| Montemarone     | 4                 | 4    | 3              | 3     | 20             | 23    | 10             | 10    |
| Pozzani         | 12                | 15   | 40             | 40    | 80             | 120   | 120            | 150   |
| Santa San Bruno | 25                | 25   | 8              | 8     | 36             | 36    | 20             | 20    |
| Vibo Valentia   | 120               | 320  | >1000          | >1000 | >1000          | >1000 | >1000          | >1000 |

Tab. 5. Tempi di ritorno (anni) dell'evento climatico (\*) per le stazioni di Mongiana e Montemarone-Caldesi.

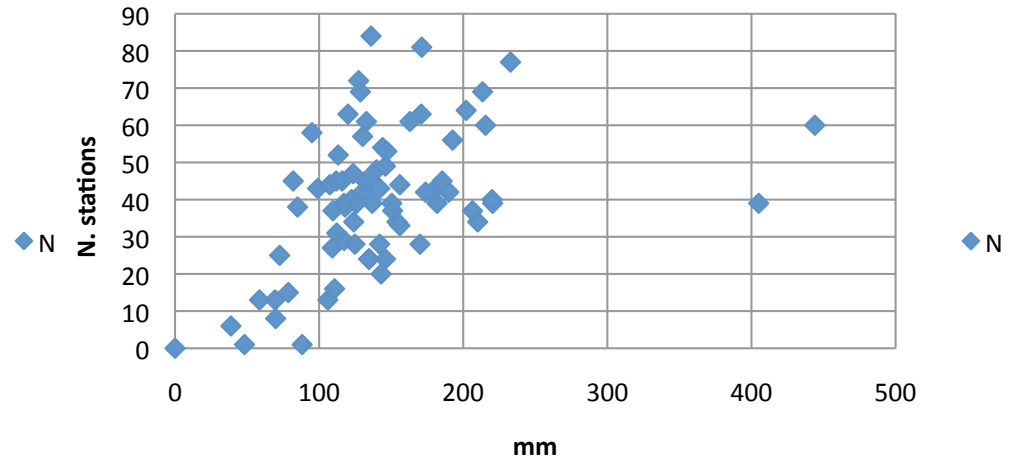
↑ T = 28000

# RELATION BETWEEN RAINFALL INTENSITY AND NUMBER OF STATIONS (Calabria region, Italy)

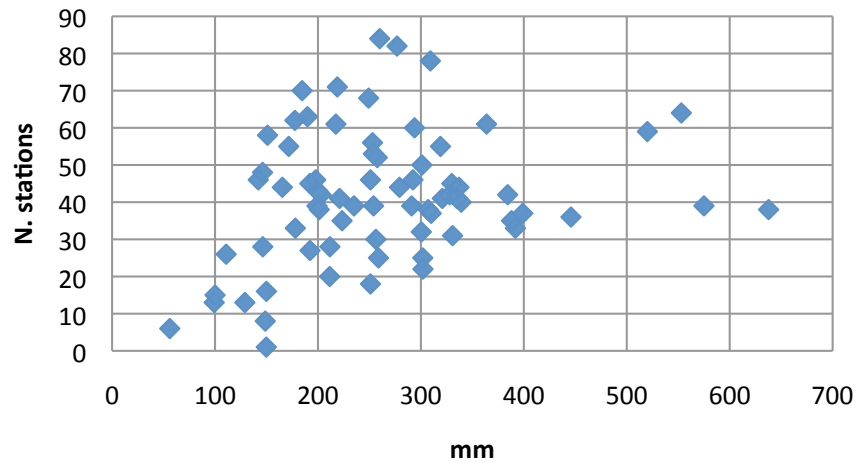
## 1H rainfall



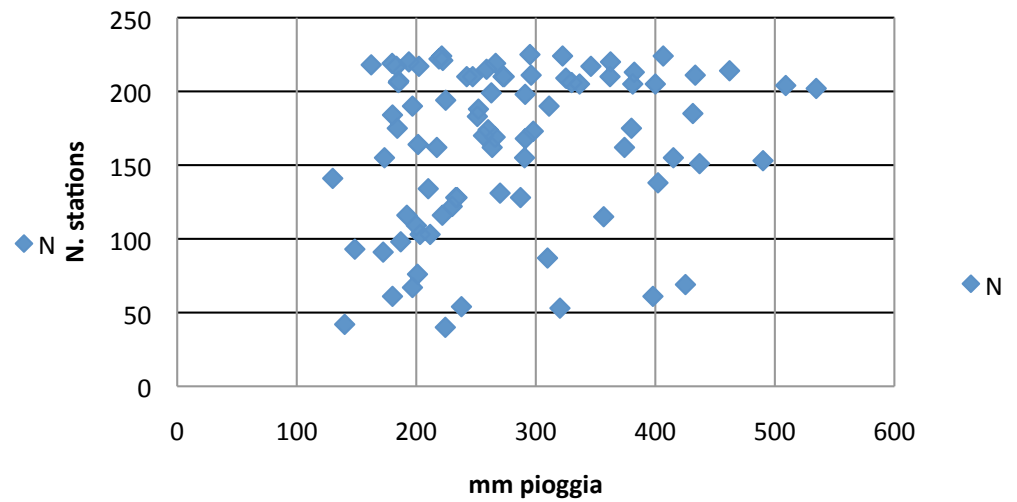
## 6H rainfall



## 24H rainfall



## Daily rainfall



**Point 1 conclusion:**(Possible weakness of short rainfall series in standard regional analysis (Italian case).

- For short rainfall series, also in presence of a sufficient number of stations, regional rainfall information may be much smaller than the appearances: about 10-15% of the total. (obviously depending on rain gauges density).
- As consequence, selection of homogeneous regions and statistical inference may lead to meaningless results.
- Failure to evaluate real maximum rainfall, expecially for small basins, may lead to overestimate the return period (or underestimate rainfall) with serious consequences in planning and design.

**Point 2:** (Search regional rainfall homogeneity using atmospheric fields)

## **REGIONAL HOMOGENEITY AND METEOROLOGICAL INDEXES**

In the case of poor rainfall historical series, selection of homogeneous region may be pursued using meteorological indexes.

Meteorological indexes must be selected according to:

- the ability to represent physical features
- continuity in time and easy computation
- possibility to build sampling data series which can be inferred with geo-statistical tools

Selected meteorological indexes are: (from ERA40 ECMWF archive, 21 layers  
0.25 x 0.25 degree resolution))

- **CAPE: Convective Available Potential Energy (convective rainfall)**
- QD : Q-Vector Divergence (frontal rainfall)
- VIMF : Vertically Integrated Moisture Flux (mean direction and intensity)



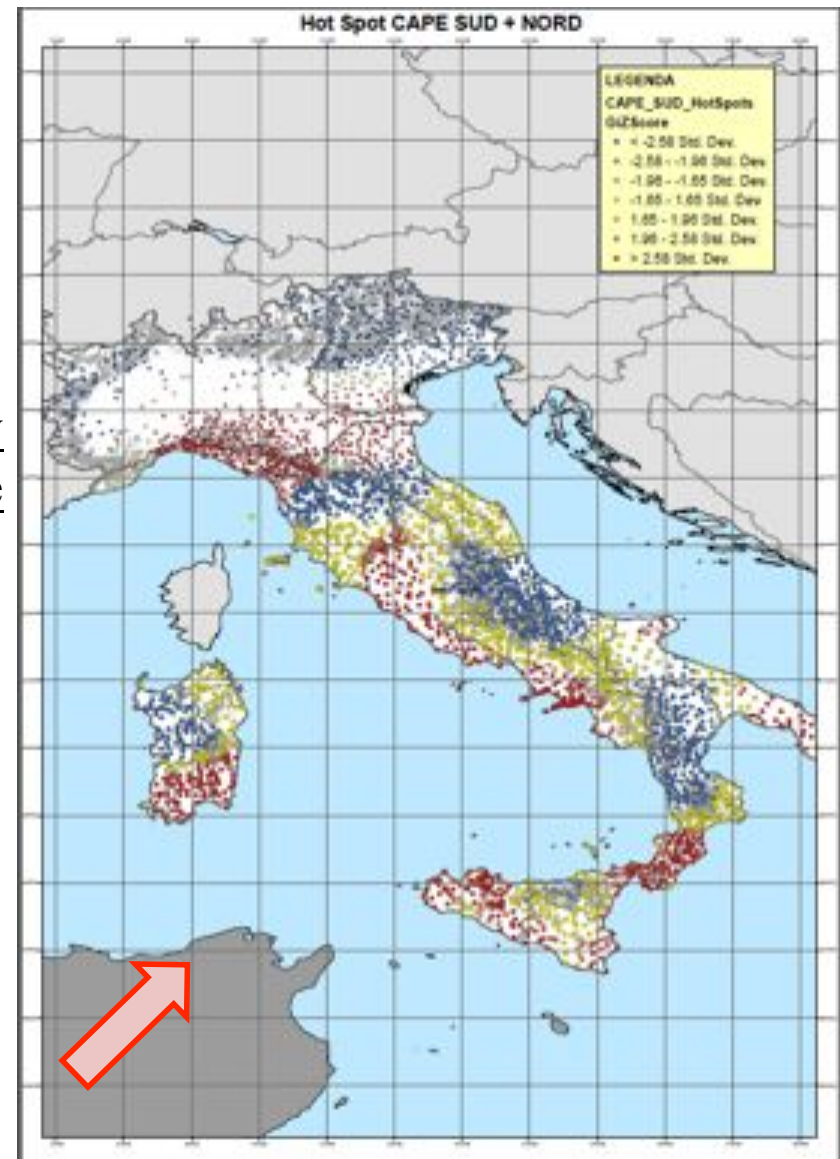
## CAPE: Convective Available Potential Energy

$$CAPE = g \int_{LFC}^{EL} \frac{T_p - T_e}{T_e} dz \cong g \sum_{LFC}^{EL} \frac{T_p - T_e}{T_e} \quad [\text{J/kg}]$$

$$T_v = T \cdot \left(1 + w \frac{R_v}{R_d}\right) / (1 + w)$$

Index able to quantify the thermodynamic instability of deep convection associated with convective rainfalls

Hot Spot results for frequency over the median values of CAPE .  
Sampling data from 1959 to 1992

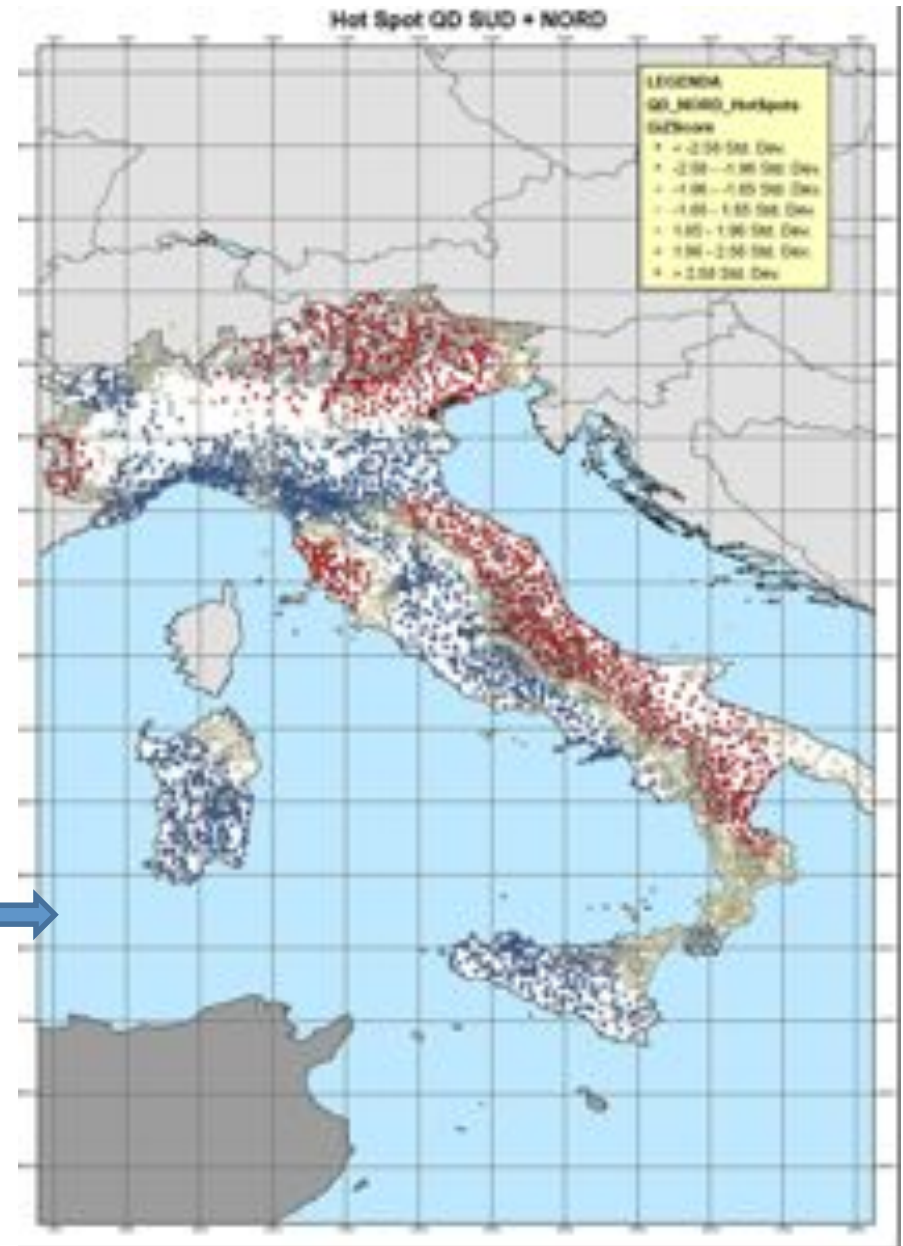


## QD: Divergence of the vector Q

$$Q_x = -\frac{R}{\rho} \frac{\partial v_g}{\partial x} \cdot \nabla T \quad Q_y = -\frac{R}{\rho} \frac{\partial v_g}{\partial y} \cdot \nabla T$$

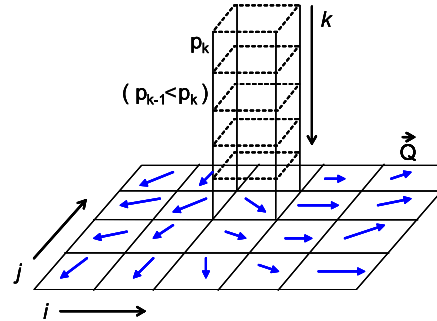
QD evaluate the presence of dynamic instability.

Hot Spot results for frequency over the median values of QD .  
Sampling data from 1959 to 1992



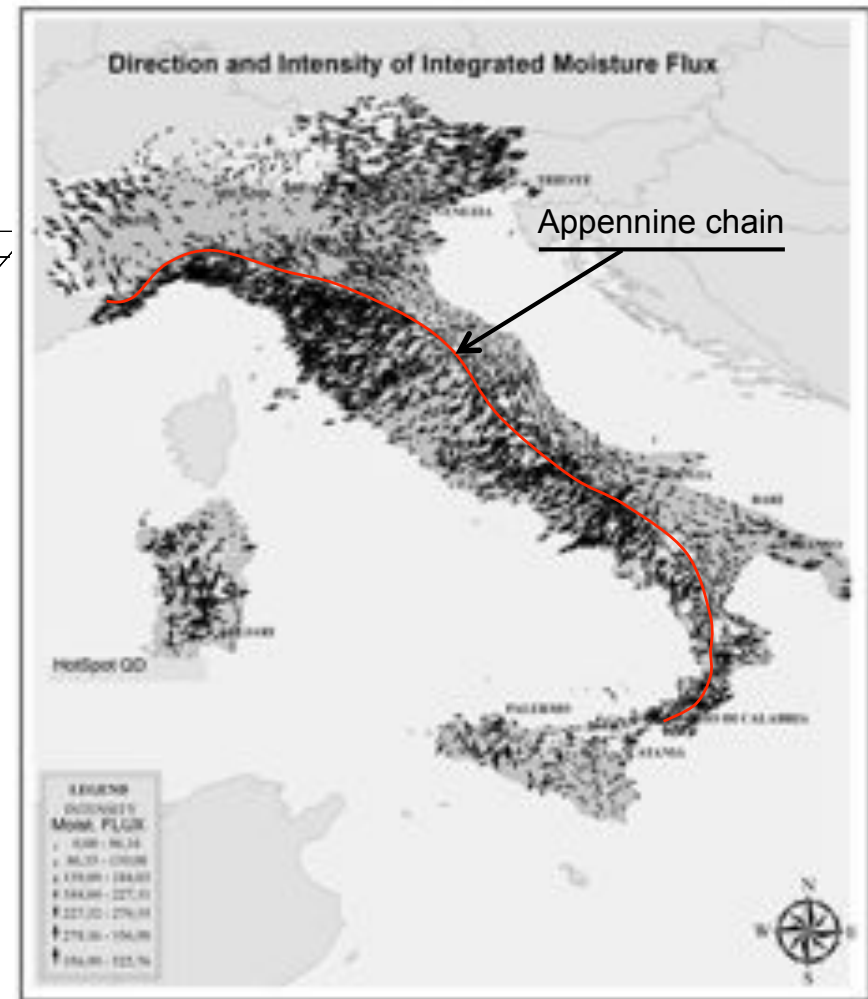
## VIMF: Vertically Integrated Moisture Flux

$$\vec{Q} = (Q_u, Q_v) = -\frac{1}{g} \int_{p_s}^{p_r} q \vec{V} dp$$



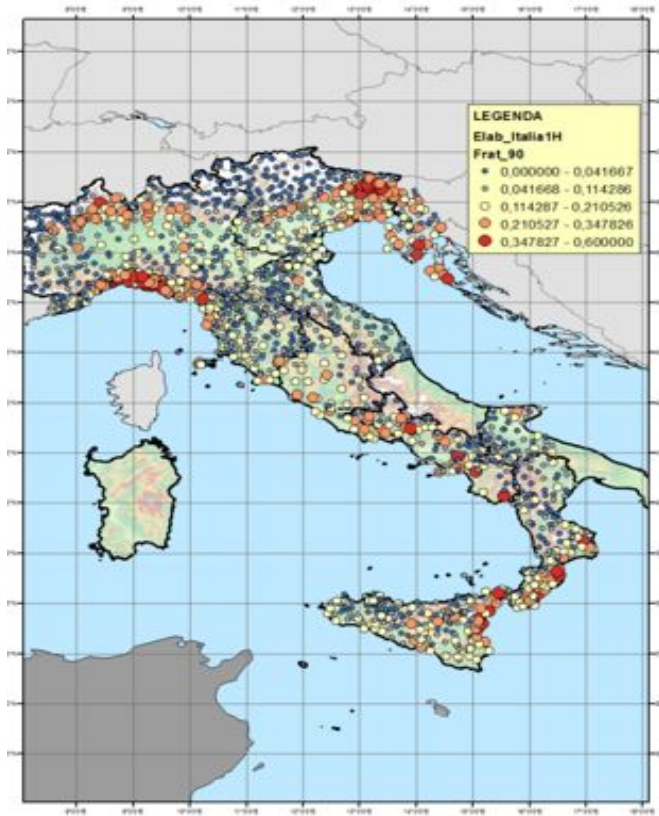
The Vertically Integrated Atmospheric Moisture Flux, describe the synoptic transport of vapor in the atmosphere. It is a fundamental parameter in the hydrological balance and for the feeding of extreme events.

Direction and intensity of VIMF based on wind maximum direction frequency.



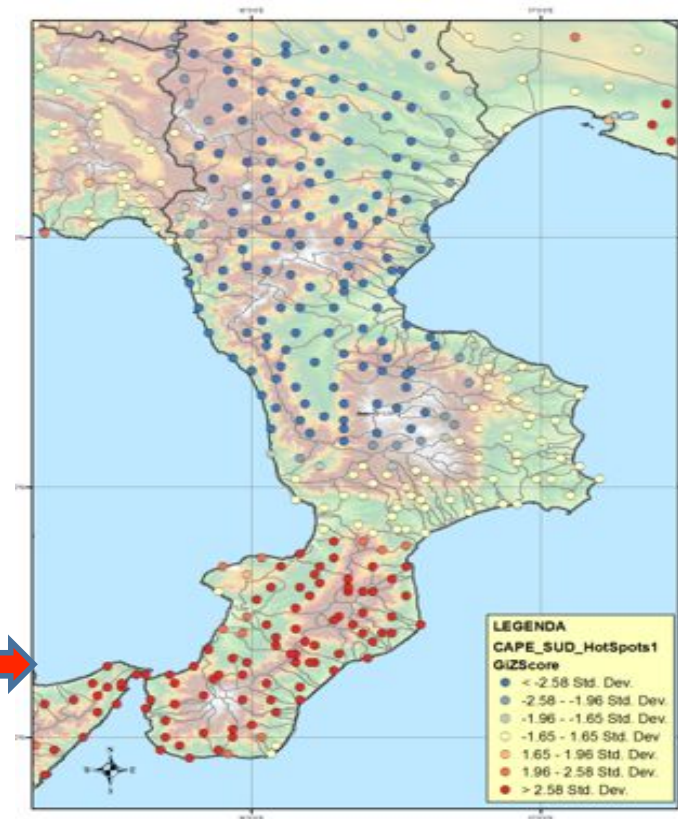
**Point 3:** (Proposition of an areal distribution for maximum annual 1H short rainfall)

Results of Hot Spot analysis on CAPE index are used to delimitate <homogeneous areas> for short rainfall of 1H.



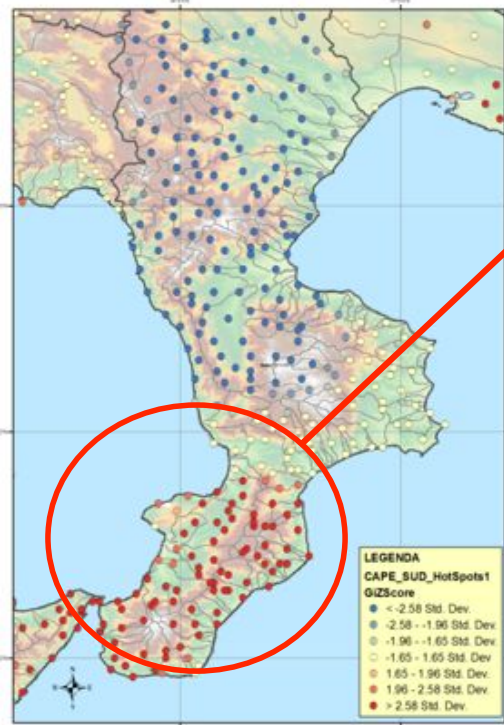
← Frequency spatial distribution of max annual rainfall of 1H over median value

Hot Spot results for frequency over the median value of CAPE index →



- High Z-score (HOT SPOT intense clustering of high values)
- Low Z-score (COLD SPOT intense clustering of low values)

# Results of homogeneity test for selected homogeneous region using CAPE index for 15 rainfall series

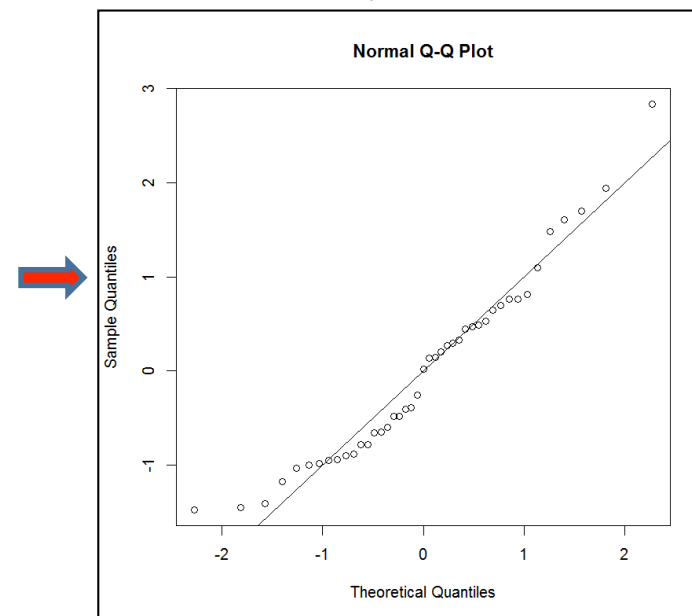


|                              |       |
|------------------------------|-------|
| STANDARDIZED TEST VALUE H(1) | -0.44 |
| STANDARDIZED TEST VALUE H(2) | -2.00 |
| STANDARDIZED TEST VALUE H(3) | -2.06 |

|                    |                   |         |
|--------------------|-------------------|---------|
| GEN. LOGISTIC      | L-KURTOSIS= 0.216 | 0.06 *  |
| GEN. EXTREME VALUE | L-KURTOSIS= 0.183 | -2.03   |
| GEN. NORMAL        | L-KURTOSIS= 0.169 | -2.93   |
| PEARSON TYPE III   | L-KURTOSIS= 0.144 | -4.57   |
| GEN. PARETO        | L-KURTOSIS= 0.103 | -7.13   |
| TCEV DISTRIBUTION  | L-KURTOSIS= 0.201 | -0.91 * |

While CAPE index, in the delimited region is normally distributed with low s.d., we consider it CONSTANT. The hypothesis of constancy of CAPE, if transfer - red to rainfall, **means that also extreme short rainfall have the same distribution all over the region.**

Normality test for CAPE



## SUPER-HOMOGENEITY AND AREAL DISTRIBUTION

If the mean of maximum annual short rainfalls is CONSTANT too (\*), we may define a UNIQUE distribution all over the super-homogeneous region.

- The regional sampling data set is build considering, year-by-year, the maximum short rainfall height recorded in the region.
- Areal parameters are estimated from a single sample site with length equal to the recorded number years.
- The distribution  $F_A(X)$  represent the probability of not excideence of  $X$  all over the region  $A$ .
- To evaluate the at-site probability we need to introduce the dimension of cell rainfall associated to the  $X$  rainfall.

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(\*) High values of CAPE identify high frequency of convective rainfall associated with cumulonimbus. The rainfall intensity associated to this kind of cloud, which can reach the stratosphere is poorly affected by orography, so far, we may consider frequency and distribution of extreme rainfall constant too.

## RELATION BETWEEN CELL SIZE AND RAINFALL INTENSITY

Distribution of rainstorm cells dimension is of great interest in attenuation models of radio transmission.

For a cell of radius  $D$ , relation rainfall intensity  $X$  versus  $D$  are commonly presented in literature as a power function:

$$D = \alpha X^\beta$$

$\alpha$  and  $\beta$  are related to the climate of the region and may be estimated using radar data.

$$A(X_i) = \pi D^2$$

The cell dimension  $A(X_i)$  for a rainfall event of height  $X_i$ , is used to evaluate the area of the “active region” equal to the mean value of  $A(X_i)$  multiplied for the yearly mean number of stations ;

$$A_c = \bar{A} * NS$$

$A_c$  represent the real portion of the regional area, interested by maximum rainfall events, which is used to evaluate distribution parameters.

## At-site estimation $F_p(X)$ starting from areal distribution $F(X)$

Estimation of  $F_p(X)$  starting from the areal distribution is here pursued in a simple way (it is under revision)

- given  $X$ , the corresponding cell area  $A_p$  is evaluated using the relation:

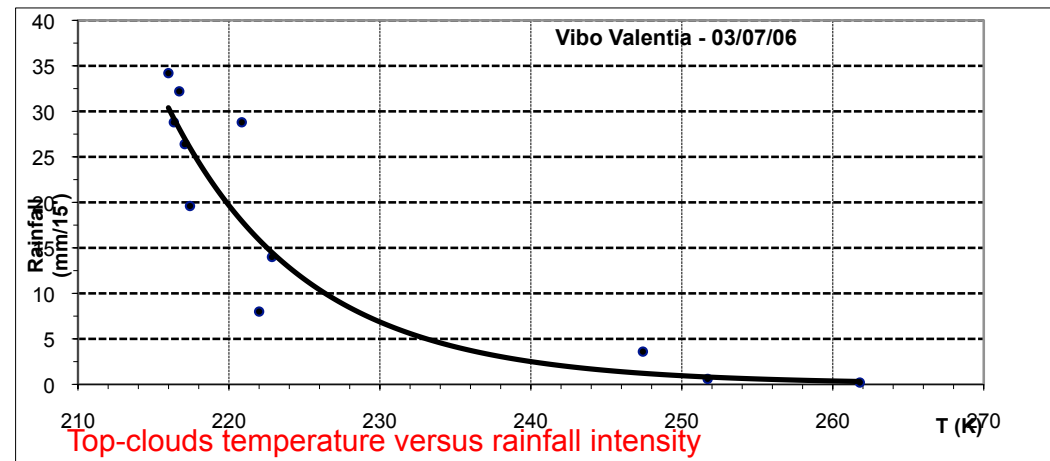
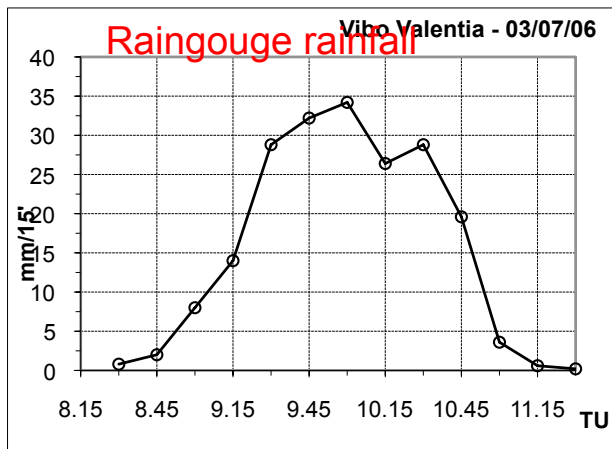
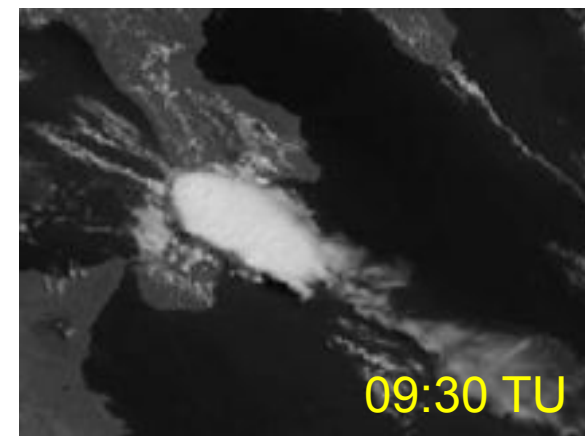
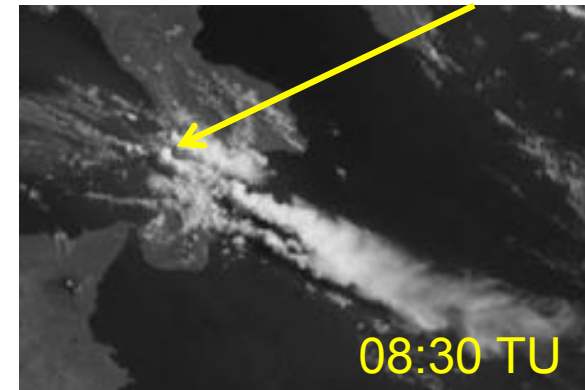
$$D = \alpha X^\beta$$
$$A_p = \pi D^2$$

If the areal distribution  $F(X)$  is evaluated using the “active areal distribution”  $A_C$  then the probability that event hit an area equal  $A_p$  is:

$$F_p(X) = F(X) * A_p / A_C$$



**POINT 4.** (Vibo Valentia flood events 3/7/2006)



# Vibo Valentia results

## AREAL ESTIMATION

**TCEV** parameters (evaluated considering 71 years) Mean number of station for year: NS = 25


$$\vartheta_1 = 13.456$$

$$\vartheta_2 = 39.457$$

$$\lambda_1 = 34.195$$

$$\lambda_2 = 1.568$$

**Areal return period:**  $F_A(X \leq 132.2) = 0.96$   $T = 1/(1-F) = T_{132.2} = \mathbf{25}$  years

**Area of the active region:**  $A_c = 554 \text{ km}^2$   
  
 $T_A = \mathbf{25}$  years (\*)

## AT-SITE ESTIMATION

Cell size:  $D(130.2) 55 * R^{-0.455}$

**Cell area:**  $A_p = 28.26 \text{ km}^2$

$$T_p = T_a * A_c / A_p = \mathbf{490} \quad (\ll 28.000)$$

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(\*) In the homogeneous region, in the last past 90 years we had 4 events with intensity greater than 132 mm.

## CONCLUSION

- Due to the small dimension of the rain cells associated with extreme events, the probability of a rain gauge to intercept the maximum rainfall is very low.
- Index method procedure for short rainfall, may overestimate return period of extreme precipitation .
- Use of meteorological information may be very useful to select homogeneous regions in presence of scarce rainfall data.
- For short rainfall, if the CAPE index may be considered constant, it is possible to hypothesize, a super-homogeneity and then a unique areal distribution all over the region.
- To evaluate at-point probability, a simple relation between rainfall intensity versus cells area is adopted for an attempt.
- The proposed procedure shows more realistic results in the case of very intense short precipitation.
- For the case of Vibo Valentia flood, the return period  $T$ , evaluated with the index-method is greater than **28000** years while with the proposed procedure is less than **500** years.