



FACETS OF UNCERTAINTY

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Union



International Association
of Hydrological Sciences



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5th EGU LEONARDO CONFERENCE • HYDROFRACTALS '13 • STATISTICAL HYDROLOGY—STAHY '13

The value of uncertainty in practice: Hydrologic design in a river section

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- Models: Cost-benefit analysis and Flood Frequency Analysis
- Models and uncertainty: the **UNCODE** Procedure
- Results
- Conclusions

Flood Frequency Analysis and Uncertainty

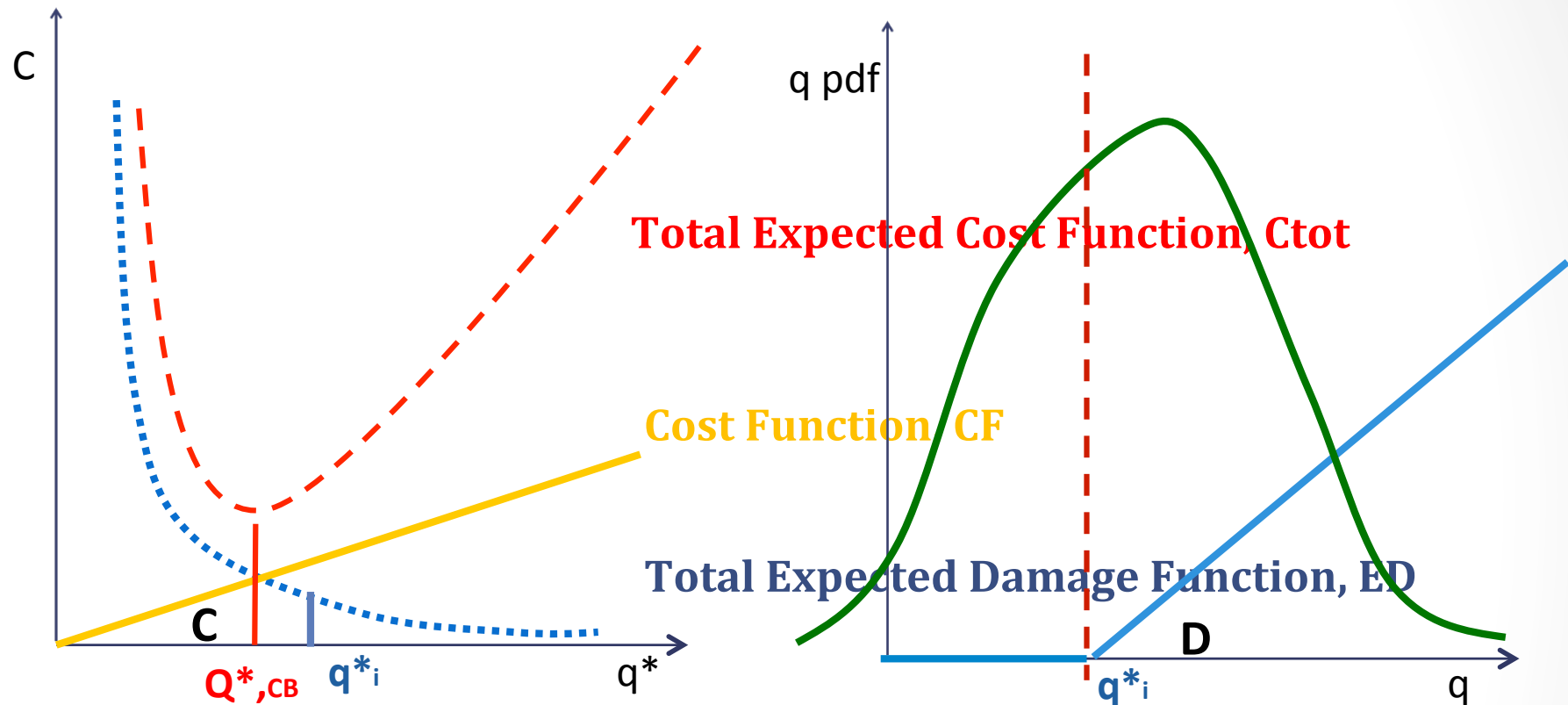


Flood Frequency Analysis is an UNCERTAIN procedure

Aim: calculate a **Design flood estimator** where **UNCERTAINTY** is taken into account

1. **Parameter** estimation
2. **Data** (sample length)

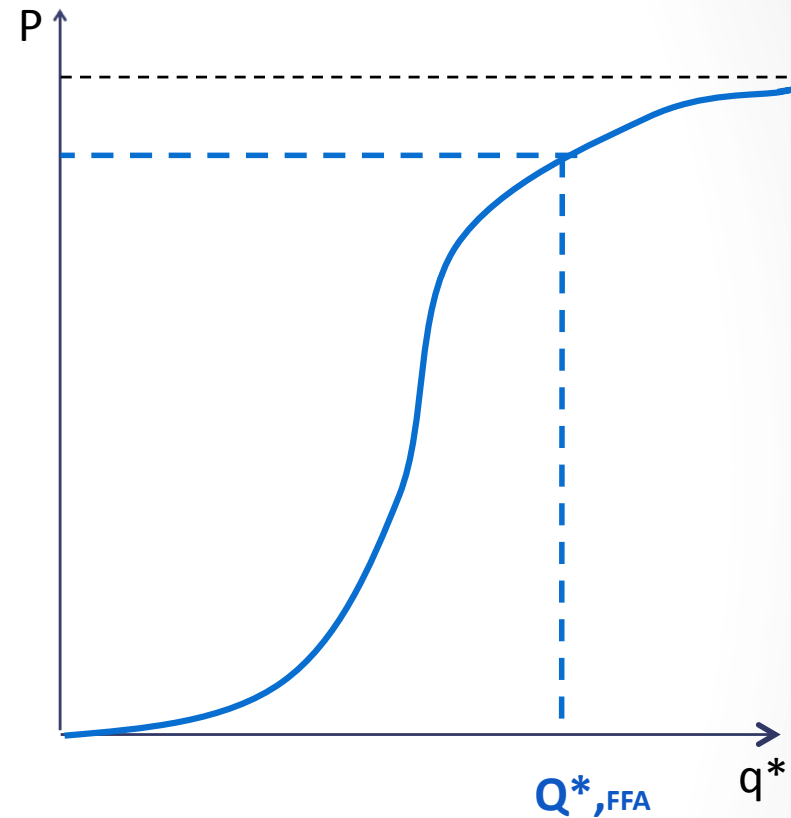
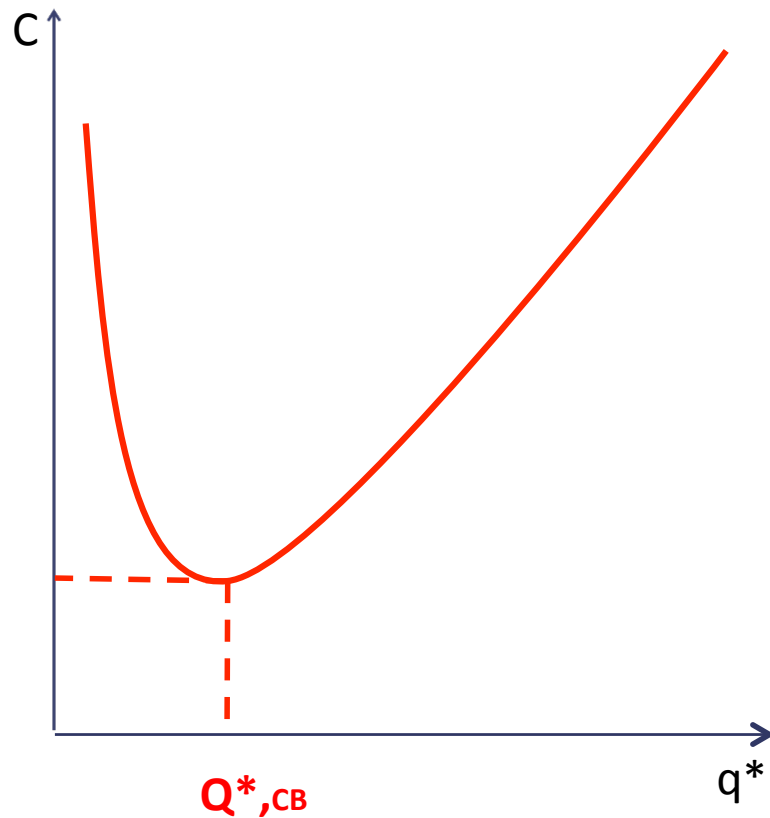
Cost-Benefit Analysis



$$C_{TOT} (q^* | \mathbf{C}, \mathbf{D}, \Theta) = CF (q^* | \mathbf{C}) + \int_{q^*}^{\infty} \Delta (q^*, q | \mathbf{D}) \cdot p (q | \Theta) dq$$

The design flood which corresponds to the minimum of total expected cost is the **DESIGN FLOOD ESTIMATOR** obtained from the Cost-Benefit Analysis.

Cost-Benefit Analysis and Flood Frequency Analysis



Analytically, it can be demonstrated that $Q^*,_{CB} = Q^*,_{FFA}$

when

Cost and Damage function are LINEAR

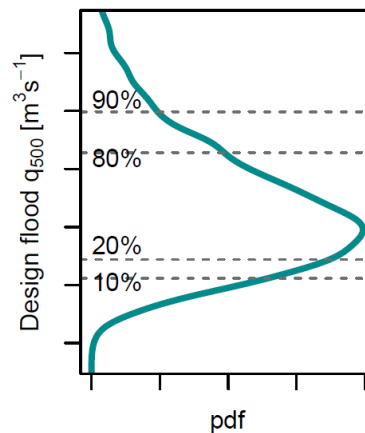
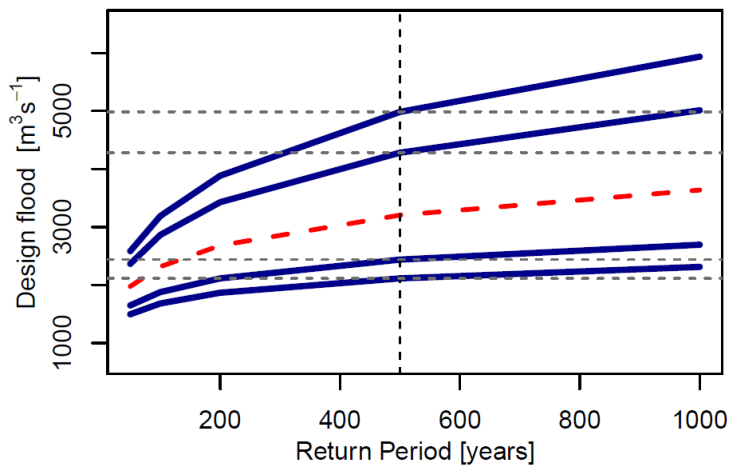
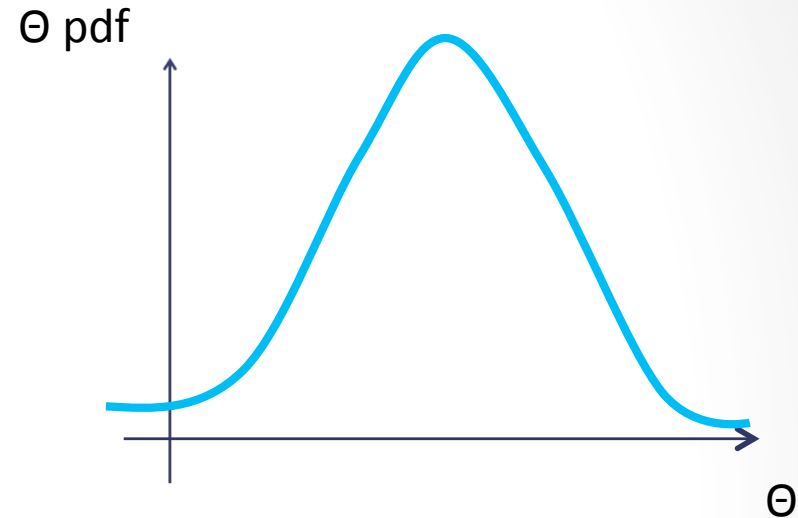
and

$$D/C = T$$

Design Flood Estimation and Parametric Uncertainty

Parameters Θ are **RANDOM variables**, so...

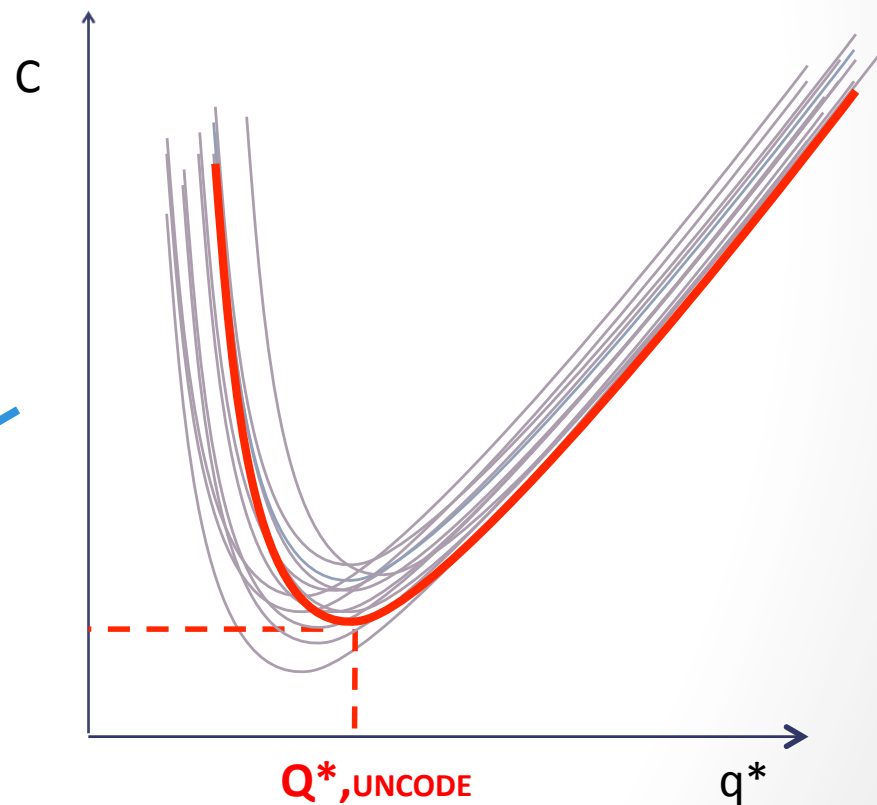
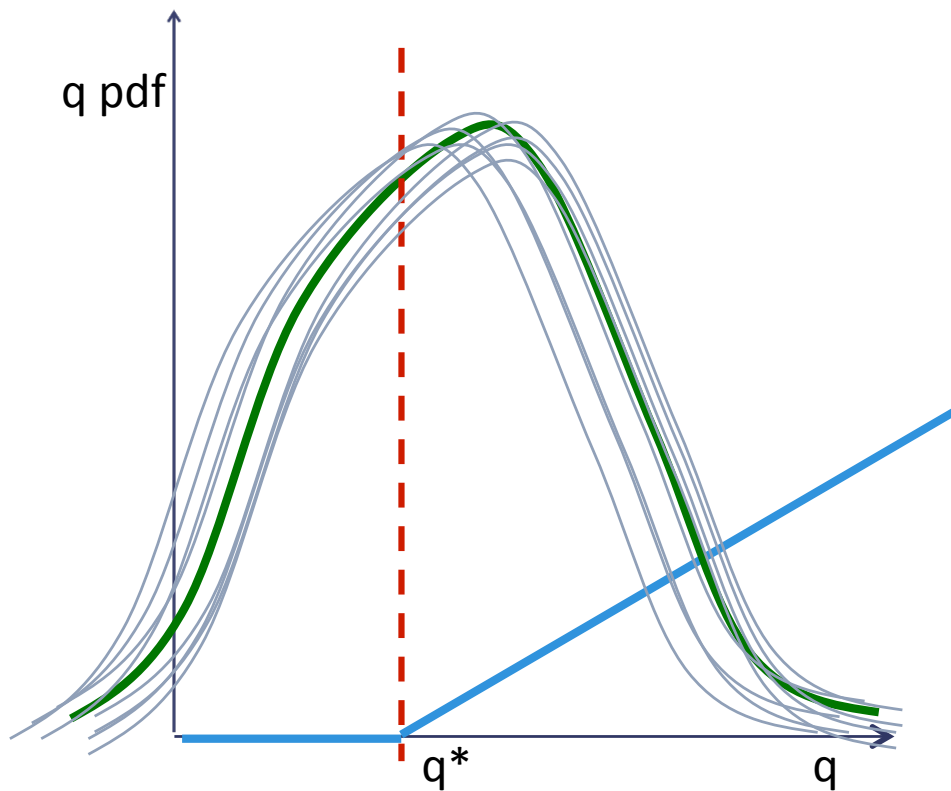
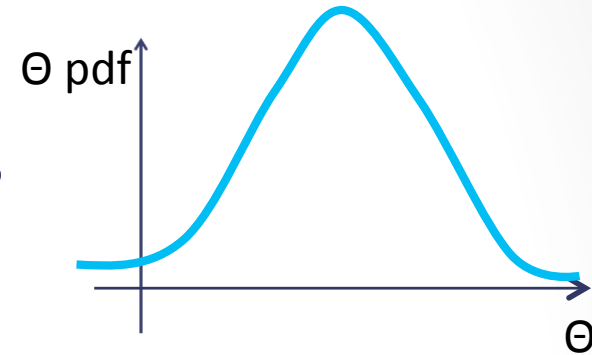
...they can be represented by a **Multivariate Probability Distribution Function**



If parameters are random variables, **Confidence bands** of the Design Flood Estimators can be obtained

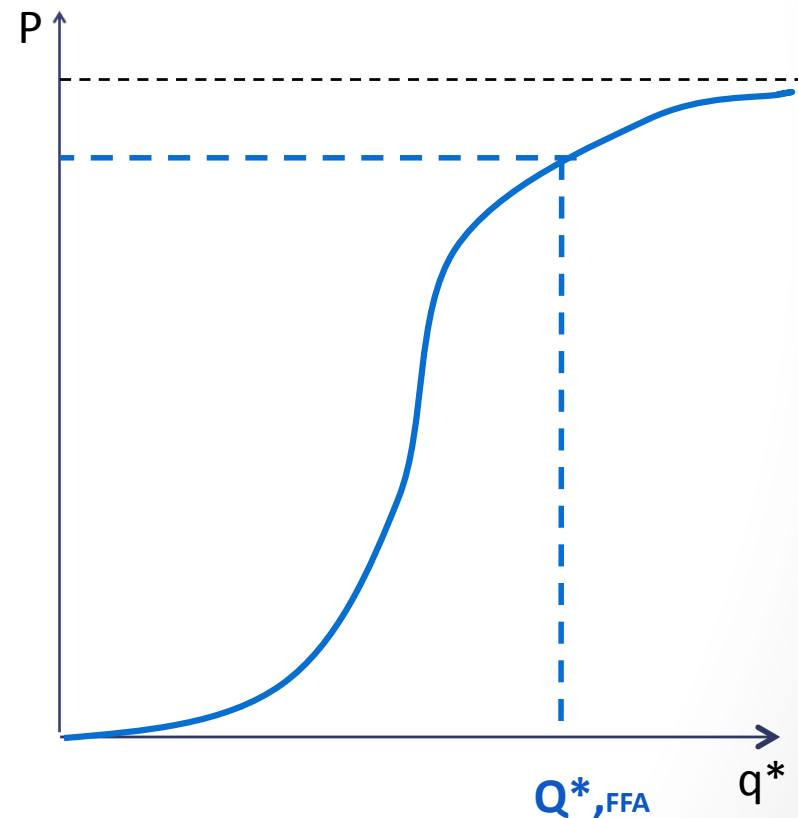
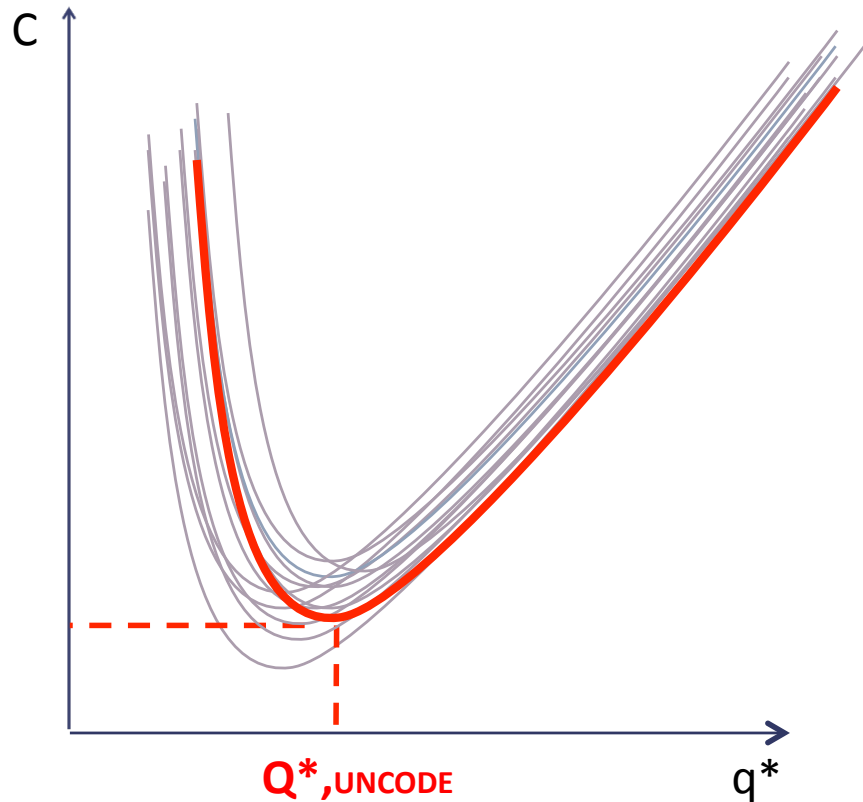
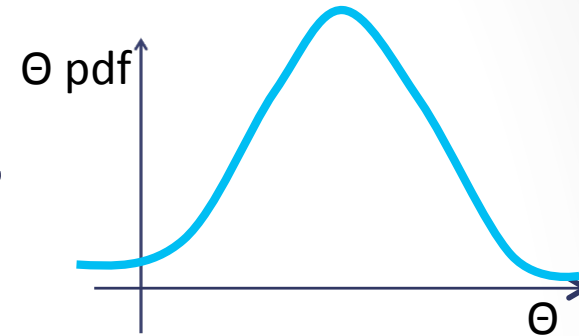
Cost-Benefit Analysis and parametric uncertainty the **UNCODE** (UNcertainty-COMpliant DEsign) Procedure

Parameters Θ are **RANDOM variables**,
SO...



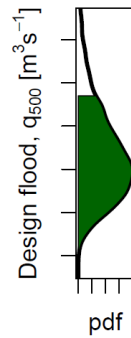
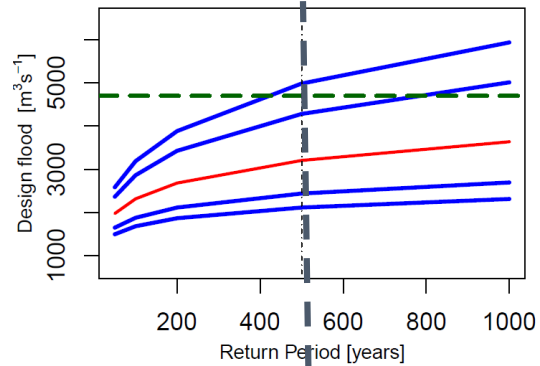
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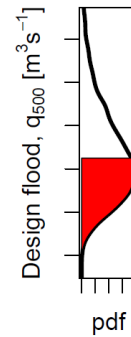
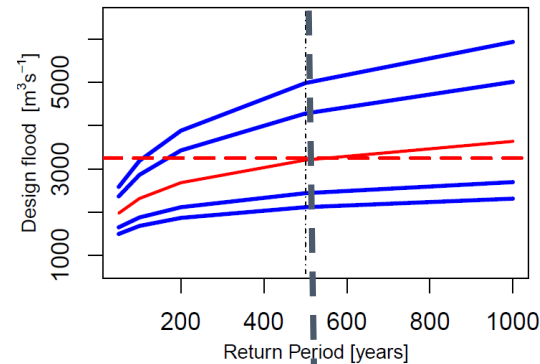


$$Q^*,_{UNCODE} \neq Q^*,_{FFA}$$

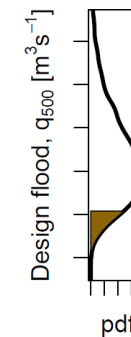
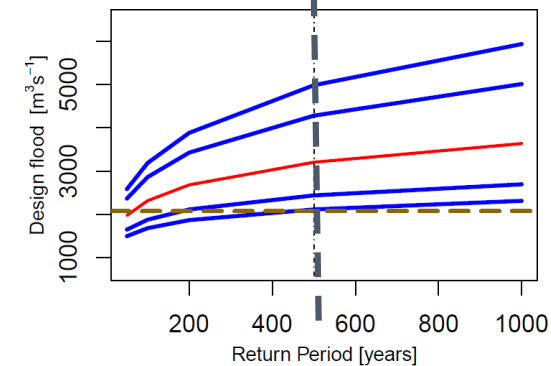
Design Flood Estimation and parametric uncertainty



$CP > 0.5 \rightarrow \gamma > 0$ [Under-estimation]

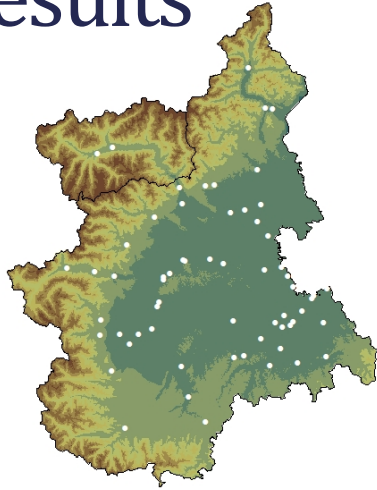


$CP = 0.5 \rightarrow \gamma = 0$

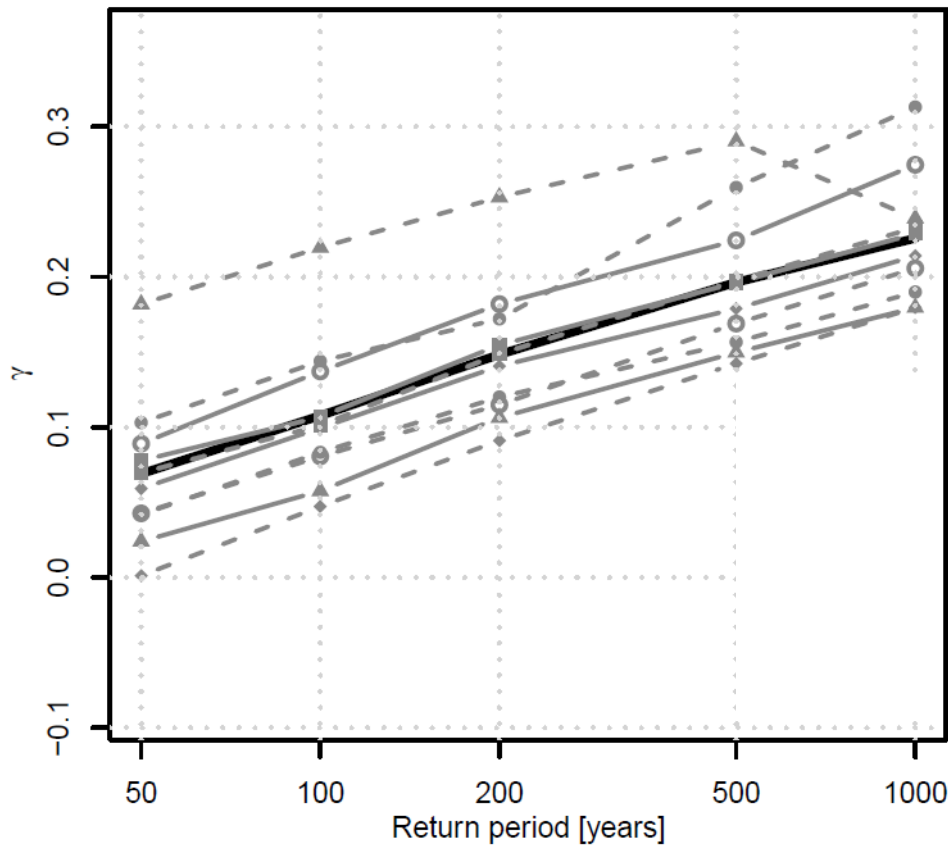


$CP < 0.5 \rightarrow \gamma < 0$ [Over-estimation]

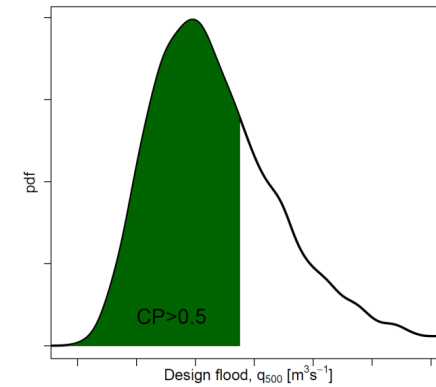
Results



The UNCODE Method has been applied in cross sections in Piemonte and Valle d'Aosta, North-West Italy

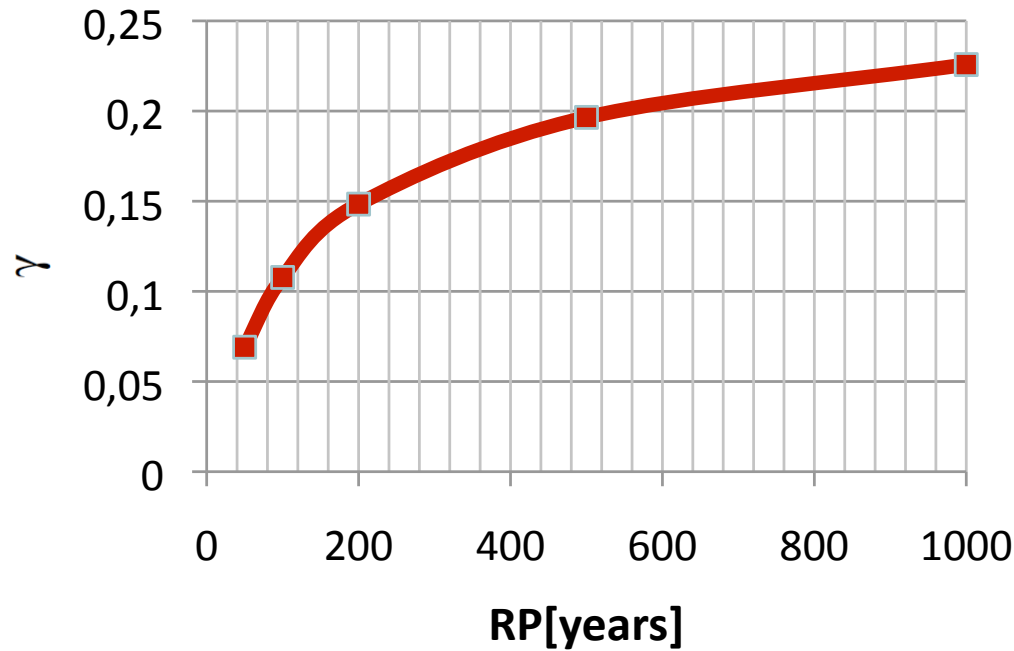


$\gamma > 0$



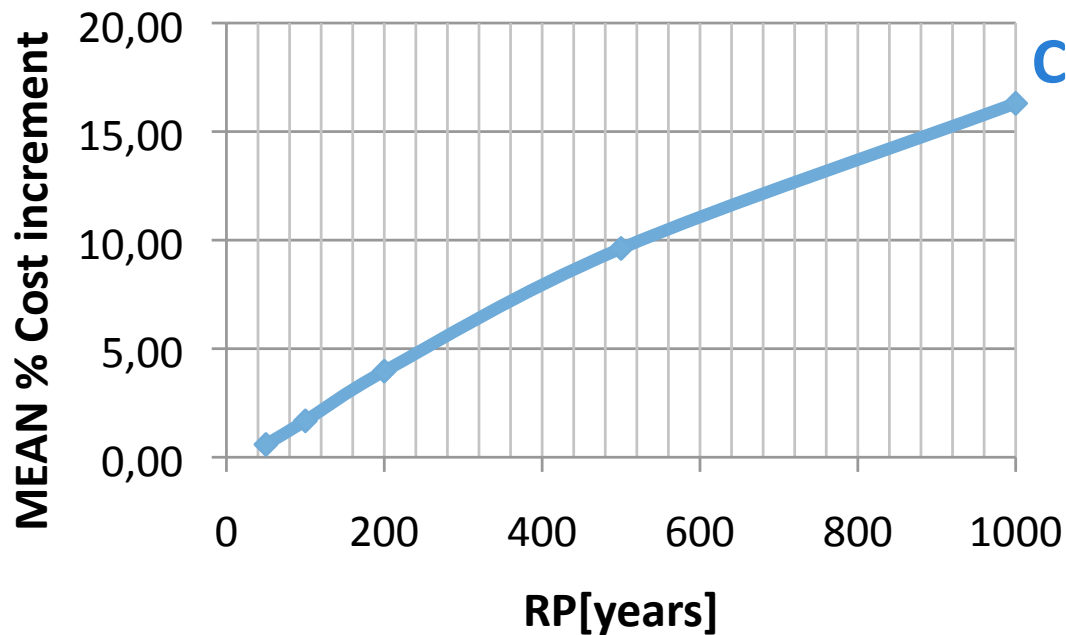
Standard Design Flood Estimators ($\gamma = 0$) seems to be under-estimated when uncertainty is taken into account

Results



Design flood estimator

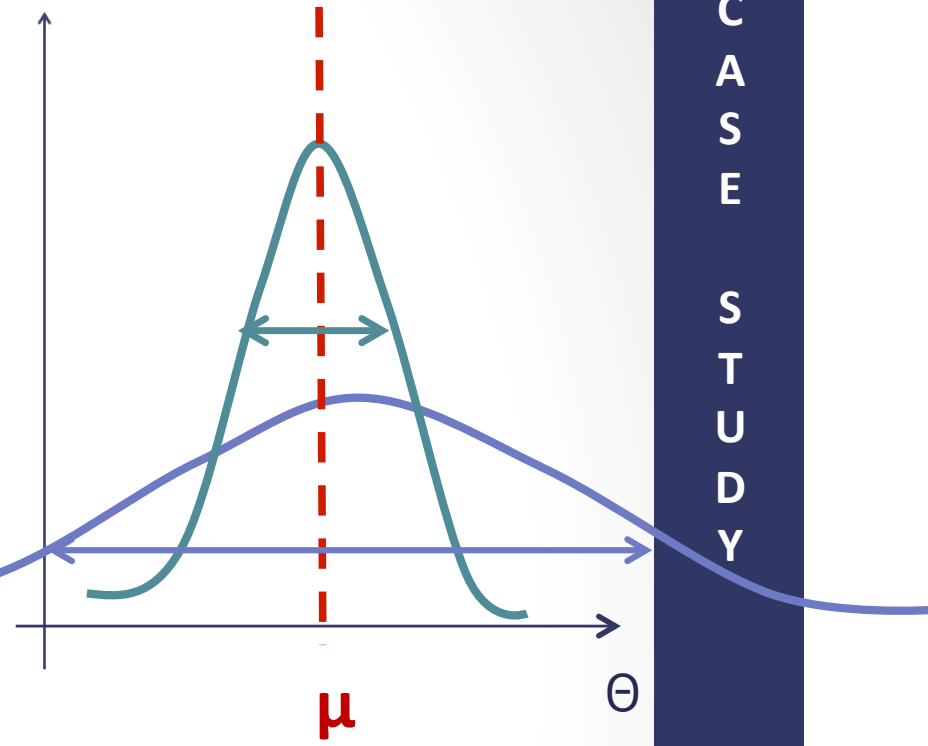
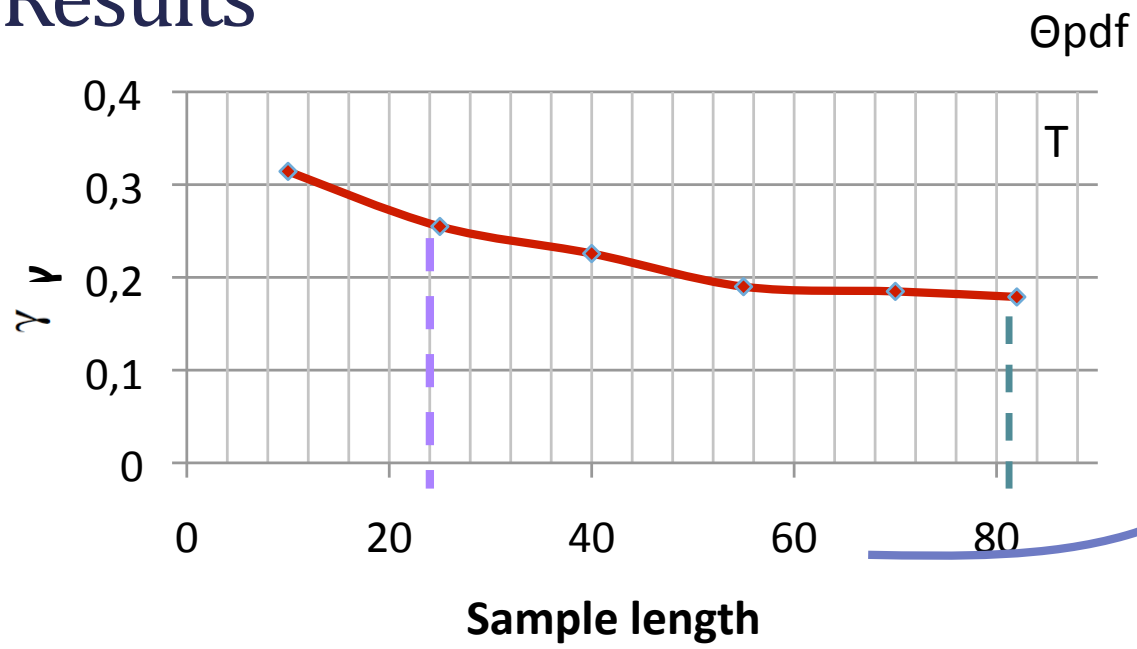
In terms of magnitude Q , the increments is up to 58 % when $T > 200$ years



Cost increment / decrement

In terms of cost, the increments is up to 15 % when $T > 200$ years

Results

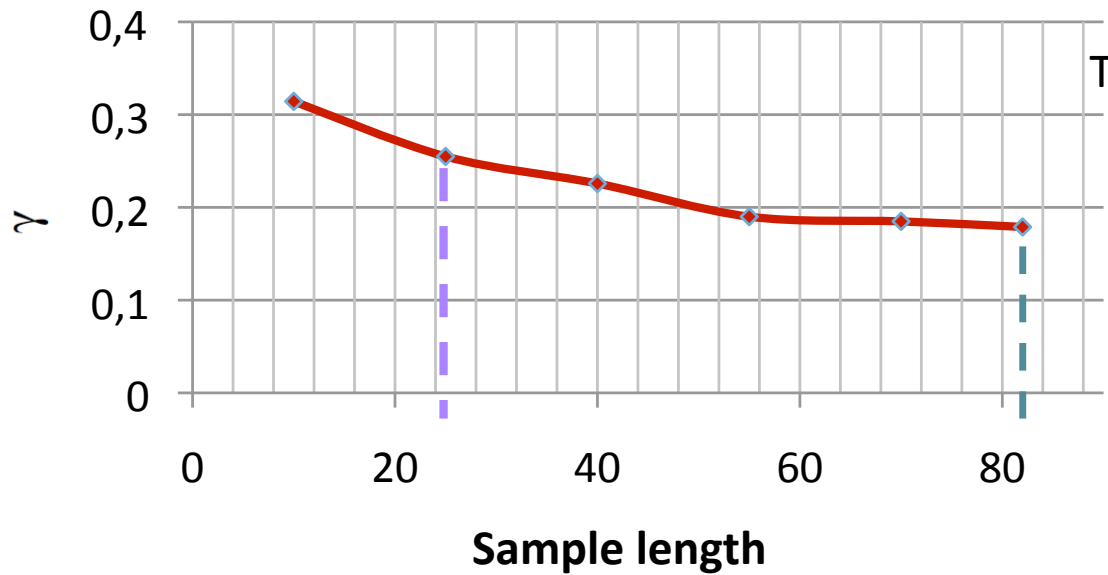


C
A
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D
Y

Results

• Small sample length entails higher value of γ



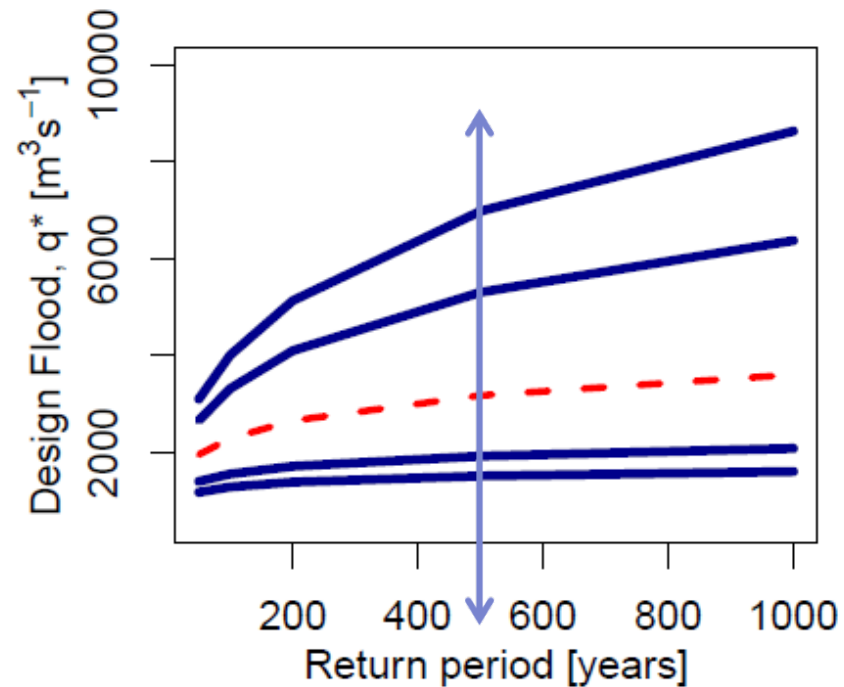
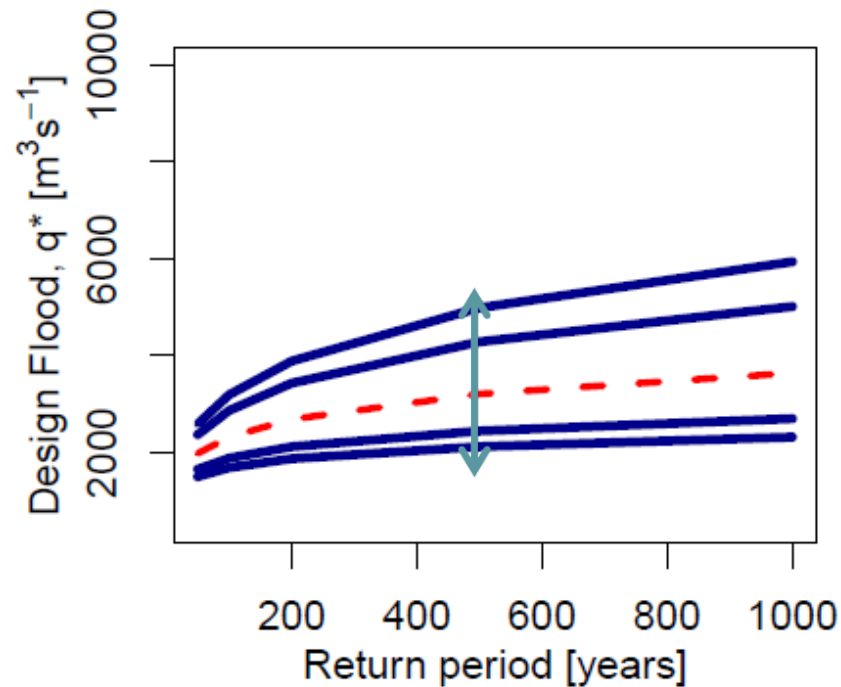
• $n=82 \rightarrow \gamma = 0.17$

• $n=25 \rightarrow \gamma = 0.26$

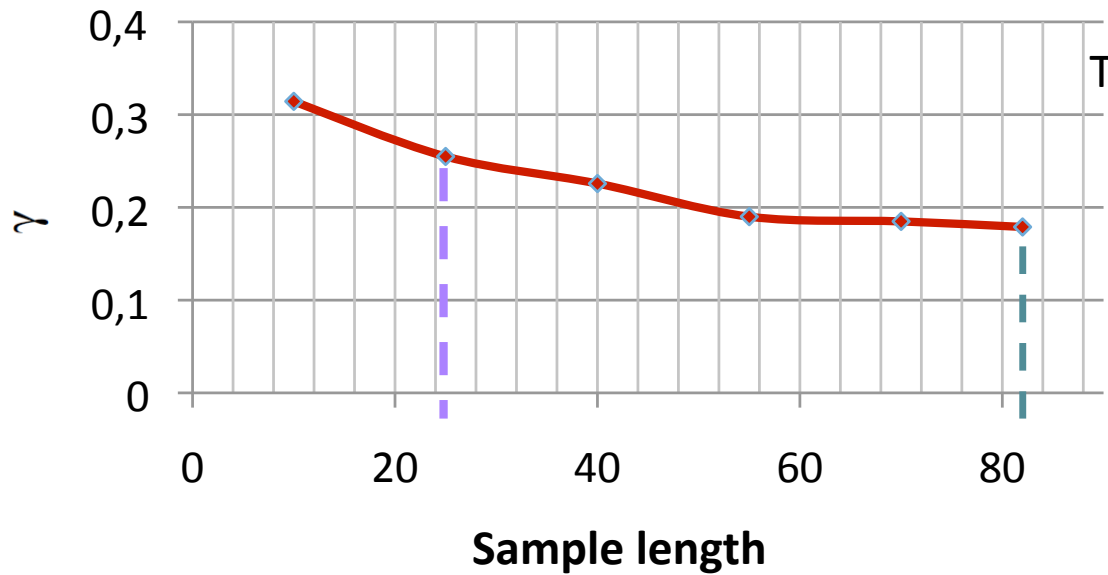
• In terms of magnitude Q:

• $n=82 \rightarrow 15\%$

• $n=25 \rightarrow 43\%$



Results



• Small sample length entails higher value of γ

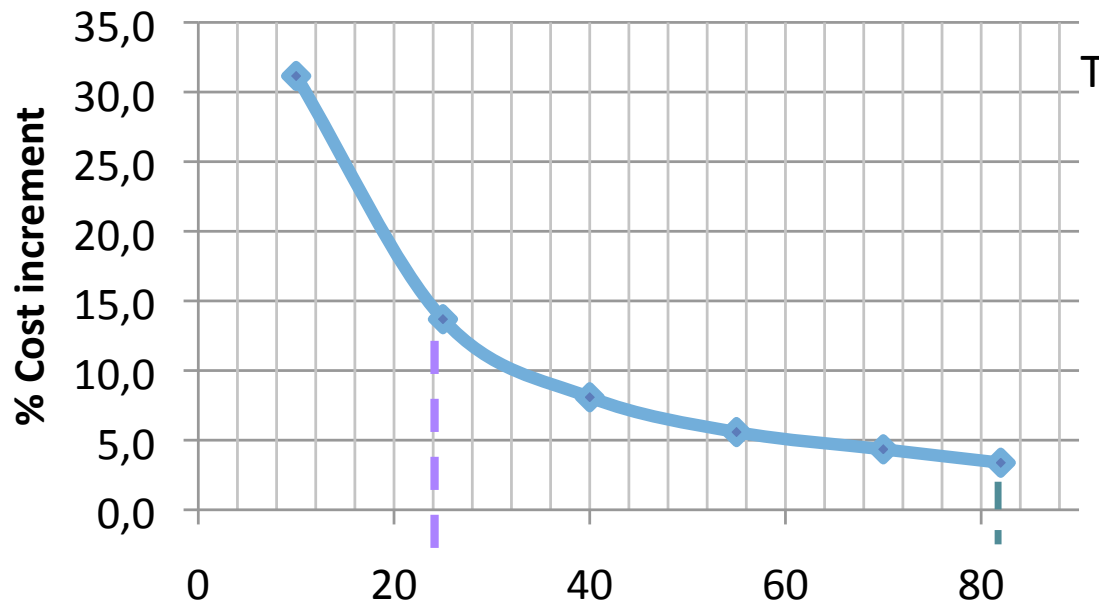
• $n=82 \rightarrow \gamma = 0.17$

• $n=25 \rightarrow \gamma = 0.26$

• In terms of magnitude Q:

• $n=82 \rightarrow 15\%$

• $n=25 \rightarrow 43\%$



• In terms of cost increment:

• $n=82 \rightarrow 4\%$

• $n=25 \rightarrow 14\%$

Conclusions

- Cost-Benefit Analysis and Flood Frequency Analysis provide the same Design Flood Estimator when
 - LINEAR cost and damage functions are applied
 - $C/D=T$
- Parametric Uncertainty plays a role and leads to consistent displacement of the UNCODE flood estimator from the standard values, especially for high return periods ($T>200y$).
- When short data samples are considered, the differences become substantial:
 - γ are larger
 - γ are calculated on larger confidence bands

Thank you for your attention

